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## Unit 9-Quadratics Review

1. Given: $f(x)=x^{2}-2 x-8$
a) Find the roots of the given equation algebraically
b) Graph of the equation.

c) Find:

- Turning Point $\qquad$
- Roots $\qquad$
- Axis of Symmetry $\qquad$
- y - intercept $\qquad$
- Domain $\qquad$
- Range $\qquad$
- Vertex form $\qquad$
- State the increasing interval graphed $\qquad$
- State the decreasing interval graphed $\qquad$

2. Directions: Answer the following questions based on this graph of a parabola:
a) Write the equation for the axis of symmetry.
b) Identify the $x$-intercepts.
c) Identify the $y$-intercept.
c) Write the quadratic equation of this graph:


In standard form: $\qquad$ In vertex form: $\qquad$
3. Find the vertex of $f(x)=-x^{2}-4 x+9$ ALGEBRAICALLY.
4. Describe how you know by looking at the equation of a quadratic function whether the graph will open upward or downward?
5. American astronauts working on a space station on the moon toss a ball into the air. The height of the ball is represented by the equation $y=-2.7 x^{2}+13.5 x+14$ where $x$ represents the number of seconds since the ball was thrown and $y$ represents the height of the ball in feet. Determine the height of the ball after 2 seconds. Show how you arrived at your answer.
6. Given the quadratic equation: $x^{2}-k x-16=0$, where -2 is one solution.
a) Find the value of $k$
b) Find the missing root
7. Write the quadratic equation in vertex form by completing the square. Then, identify the quadratic equation's turning point. $f(x)=x^{2}-2 x+8$
8. Write the quadratic equation in vertex form by completing the square. Then, identify the quadratic equation's turning point. $f(x)=2 x^{2}+36 x+170$
9. The populations of two different villages are modeled by the equations shown below. The population (in thousands) is represented by $y$ and the number of years since 1975 is represented by $x$. Lewiston village is represent by $f(x)=x^{2}-30 x+540$ Lockport village is represent by $g(x)=20 x+15$
a. Algebraically, determine which year did the villages have the same population?
b. Algebraically, determine what was the population of both cities during the year of equal population?
10. If $(x-7)$ is a factor of $2 x^{2}-11 x+k$, what is the value of $k$ ?
(1) -21
(2) -7
(3) 7
(4) 28
11. The height, $h$, of a golf ball hit into the air can be represented by the equation $h=-16 t^{2}+48 t$, where $t$ is the elapsed time.
a) Graph $h=-16 t^{2}+48 t$
b) At what time is the ball at its highest point?
c) Write the equation of the axis of symmetry.

d) Domain
e) Range $\qquad$
f) State the increasing interval graphed $\qquad$
g) State the decreasing interval graphed $\qquad$
12. What is the solution of the system of equations shown below?

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\begin{gathered}
f(x)=x-2 \\
g(x)=x^{2}-8 x+6
\end{gathered}
$$

(1) $(-1,-3)$ and $(-8,-10)$
(2) $(2,0)$ and $(-8,-10)$
(3) $(0,-2)$ and $(5,3$
(4) $(1,-1)$ and $(8,6)$
13. Which of the following equations is equivalent to $x^{2}+14 x-14=0$
(1) $(x+7)^{2}=14$
(2) $(x+7)^{2}=63$
(3) $(x+14)^{2}=14$
(4) $(x+14)^{2}=63$
14. What are the vertex and axis of symmetry of the parabola $y=x^{2}-16 x+63$ ?
(1) vertex: ( $8,-1$ ); axis of symmetry: $x=8$
(3) vertex: $(-8,-1)$; axis of symmetry: $x=-8$
(2) vertex: $(8,1)$; axis of symmetry: $x=8$
(4) vertex: $(-8,1)$; axis of symmetry: $x=-8$
15. Let $f$ be the function represented by the graph below.


Let $g$ be a function such that $g(x)=-\frac{1}{2} x^{2}+4 x+3$. Determine which function has the larger maximum value. Justify your answer. (hint: find the maximum for $g(x)$ algebraically)
16. Which sketch is the correct graph for the function $y=x^{2}-5 x-6$ ?

(1)

(2)

(3)

(4)
17. Each time Juanita bowls, her score increases by $5 \%$ of her previous score. If her initial score is represented by a, which equations shows this relationship?
a) $y=a(1.5)^{x}$
b) $y=a(1.05)^{x}$
c) $y=0.05^{x}$
d) $y=a(0.5)^{x}$
18. Ryan is given the graph of the function $y=\frac{1}{2} x^{2}-4$. He wants to find the zeros of the function, but is unable to read them exactly from the graph.
a) Find the zeros in simplest radical form.
(hint: use a specific formula)

19. What is the slope and $y$ intercept of: $x-3 y=-15$ ?
20. What is the order, from narrowest to widest graph, of the quadratic function $f(x)=-10 x^{2}, f(x)=2 x^{2}$, and $f(x)=0.5 x^{2}$ ?
(1) $f(x)=-10 x^{2}, f(x)=2 x^{2}$, and $f(x)=0.5 x^{2}$
(3) $f(x)=0.5 x^{2}, f(x)=2 x^{2}$, and $f(x)=-10 x^{2}$
(2) $f(x)=2 x^{2}, f(x)=-10 x^{2}$, and $f(x)=0.5 x^{2}$
(4) $f(x)=0.5 x^{2}, f(x)=-10 x^{2}$, and $f(x)=2 x^{2}$
21. Joey's math class is studying the basic quadratic function, $f(x)=x^{2}$. Each student is supposed to make two new functions by adding or subtracting a constant to the function. Joey chooses the functions $g(x)=x^{2}-5$ and $h(x)=x^{2}+2$. What transformations would map $f(x)$ to $g(x)$ and $f(x)$ to $h(x)$ ?
(1) shift left 5 , shift right 2
(3) shift up 5 , shift down 2
(2) shift right 5 , shift left 2
(4) shift down 5 , shift up 2
22. What is the difference when $2 x^{3}+x-5$ is subtracted from $6 x^{3}-x^{2}+4 x+8$ ?

