Name **Answer Key**

Unit 3 Review HW#____

Solve the following system algebraically and check.

1. $y = 3x + 8$

$4x + 2y = 6$

$4x + 2(3x + 8) = 6$

$4x + 6x + 16 = 6$

$10x + 16 = 6$

$\underline{\quad -16 \quad -16}$

$\dfrac{10x}{10} = \dfrac{-10}{10}$

$\boxed{x = -1}$

$y = 3(-1) + 8$

$y = -3 + 8$

$\boxed{y = 5}$

$(-1, 5)$

Ch

$5 = 3(-1) + 8$

$5 = -3 + 8$

$5 = 5 \checkmark$

Ch

$4(-1) + 2(5) = ($

$-4 + 10 = 6$

$6 = 6 \checkmark$

Solve the following systems of inequalities graphically and check.

2. $y < 1$ and $y \le 2x - 3$

↓

horizontal

dashed

below

$m = \dfrac{2}{1}$

$b = -3$

Solid

below

$(4, 0)$

$y < 1 \qquad y \le 2x - 3$

$0 < 1 \checkmark \qquad 0 \le 2(4) - 3$

$\qquad\qquad 0 < 8 - 3$

3. $2x - 3y \le 12$ and $x + 5y < 20$

$\underline{-2x \qquad -2x}$

$\dfrac{-3y}{-3} \le \dfrac{-2x}{-3} + \dfrac{12}{-3}$

$\boxed{y \ge \dfrac{2}{3}x - 4}$

$m = \dfrac{2}{3} \quad b = -4$

$\underline{-x \qquad -x}$

$\dfrac{5y}{5} < \dfrac{-x}{5} + \dfrac{20}{5}$

$\boxed{y < -\dfrac{1}{5}x + 4}$

$m = -\dfrac{1}{5} \quad b = 4$
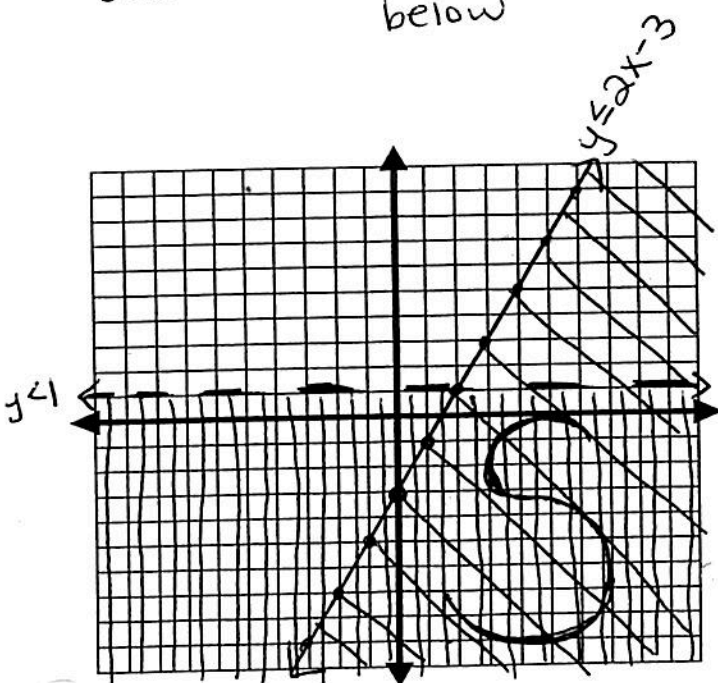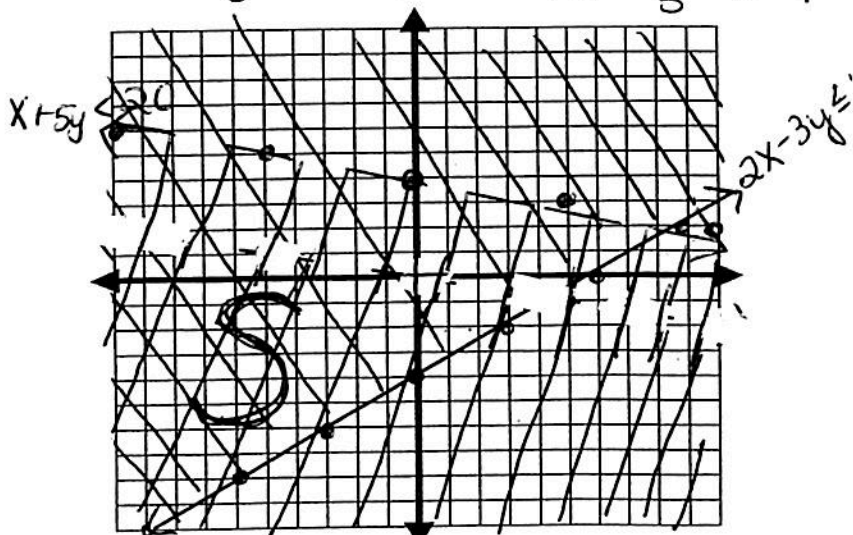
$(-1, -2)$

$2(-1) - 3(-2) \le 12$

$-2 + 6 \le 12$

$4 \le 12 \checkmark$

$-1 + 5(-2) < 2$

$-1 - 10 < 20$

$-11 < 20 \checkmark$

Solve the following word problems algebraically. Be sure to include a legend, equations, and solution.

4. According to a recent report, John Paul Ofwono of Uganda is so tall he can pick mangoes without climbing a tree. John's height plus his father's height is 163 inches, while the difference in their heights is 33 inches. Assuming John is taller than his father, how tall is each man?

J = John's height
F = Father's height

$$J + F = 163$$
$$+ \quad J - F = 33$$
$$\overline{2J = 196}$$
$$\frac{2J}{2} = \frac{196}{2}$$
$$\boxed{J = 98 \text{ in}}$$

$$98 + F = 163$$
$$-98 \qquad -98$$
$$\boxed{F = 65 \text{ in}}$$

5. I have 30 coins of dimes and quarters that have a total value of $4.95. How many dimes and how many quarters do I have?

d = dimes
q = quarters

$$-10(d + q = 30)$$
$$.10d + .25q = 4.95$$

$$10d + 25q = 495$$
$$-10d - 10q = -300$$
$$\overline{15q = 195}$$
$$\frac{15q}{15} = \frac{195}{15}$$
$$\boxed{q = 13}$$

$$d + 13 = 30$$
$$\quad -13 \quad -13$$
$$\boxed{d = 17}$$

6. At a local video rental store, Joe rents two movies and three games for a total of $15.50. At the same time, Meg rents three movies and one game for a total of $12.05. How much money is needed to rent <u>three</u> games and one movie?

m = movie
g = game

$$1(2m + 3g = 15.50)$$
$$-3(3m + 1g = 12.05)$$

$$-9m - 3g = -36.15$$
$$2m + 3g = 15.50$$
$$\overline{-7m = -20.65}$$
$$\frac{-7m}{-7} = \frac{-20.65}{-7}$$
$$\boxed{m = 2.95}$$

$$2(2.95) + 3g = 15.5$$
$$5.90 + 3g = 15.5$$
$$-5.90 \qquad -5.9$$
$$\frac{3g}{3} = \frac{9.60}{3}$$
$$\boxed{g = 3.20}$$

※ 3 games → 3(3.20) = 9.60
1 movie → + 2.95
$10.55

7. Currently, Tyrone has $60 and his sister has $135. Both get an allowance of $5 each week. Tyrone decides to save his entire allowance, but his sister spends all of hers each week.

Let X = # of weeks

a) Write one equation representing the spending of Tyrone.

$$y = 5x + 60$$

b) Write one equation representing the spending of his sister.

$$y = -5x + 135$$

8. The senior class is sponsoring a dance. The cost of a student disk jockey is $40 and tickets sell for $2 each.

Let X = # of tickets

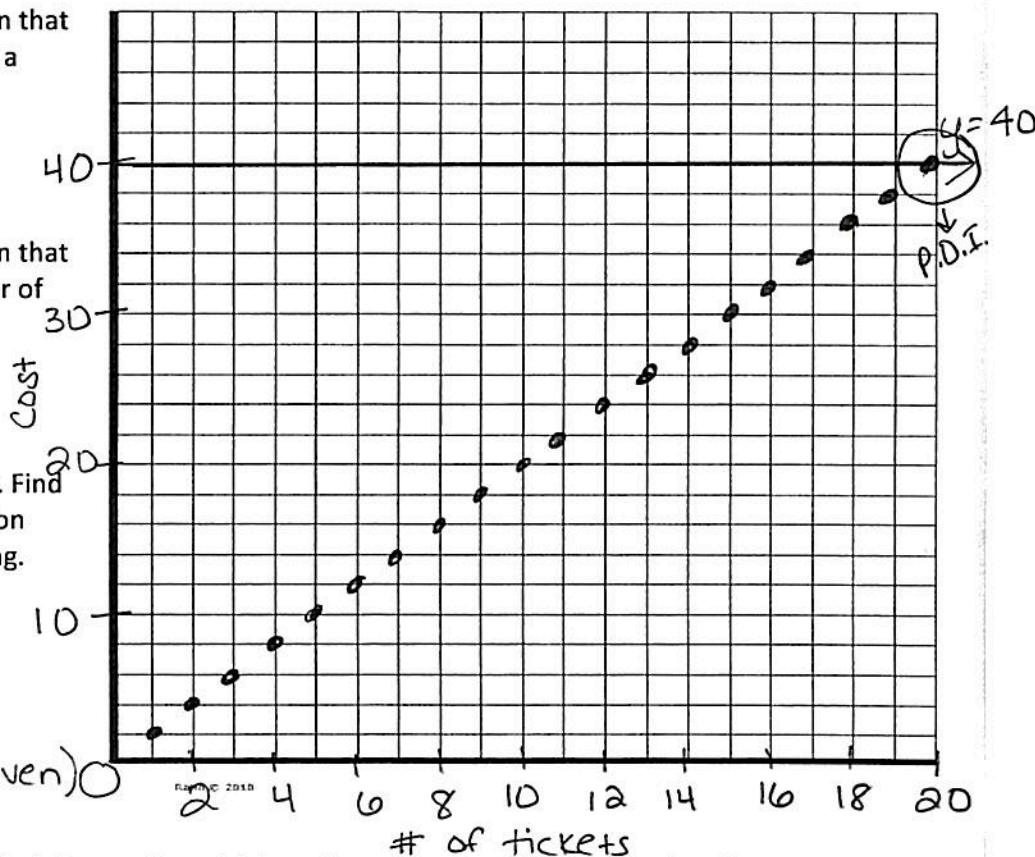a. Write a linear equation that represents the cost of a student disk jockey.

$$y = 40$$

b. Write a linear equation that represents the number of tickets sold.

$$y = 2x$$

c. Graph both equations. Find the point of intersection and explain its meaning.

$(20, 40)$
If they sell 20 tickets, they will get $40.
(They will break even)

Cost

y = 40

P.D.I.

# of tickets

d. Solve algebraically to find the number of tickets the senior class has to sell to break even.

$$y = 40$$
$$y = 2x$$
↓
Set them = to each other!

$$\frac{2x}{2} = \frac{40}{2}$$

$$\boxed{x = 20 \text{ tickets}}$$

e. A student claimed she sold $33 worth of tickets and her classmate exclaimed, "That's not possible!" Explain why.

No b/c there cannot be a "decimal" amount of tickets.

$$\frac{\$33}{2} = 16.5 \text{ tix}$$

* $y = 2x$ has finite solutions. → do not connect line!

9. Which orders pair is _not_ a solution of $4y < 3x + 5$? → plug in choices

    a. (-3,-2)

    b. (0,1)

    c. $(\frac{1}{3}, \frac{3}{2})$

    d. (1,1)

$$4\left(\frac{3}{2}\right) < 3\left(\frac{1}{3}\right) + 5$$

$$6 < 1 + 5$$

$$6 < 6 \text{ not true}$$

10. Write an inequality for the following sentences.

    a) Two less than five times a number is at least twelve. $5x - 2 \geq 12$

    b) Four times a number is less than negative eight. $4x < -8$

    c) The difference of 2 numbers is at most 40 $x - y \leq 40$

11. Using the substitution method, Ken solves the following system of equations algebraically.

$$2x - y = 5$$
$$+y \quad +y$$
$$3x + 2y = -3$$

→ $2x = 5 + y$
$$-5 \quad -5$$
$$y = 2x - 5$$

$3x + 2y = -3$

Which equivalent equation could Ken use?

    a. $3x + 2(2x - 5) = -3$

    b. $3x + 2(5 - 2x) = -3$

    c. $3\left(y + \frac{5}{2}\right) + 2y = -3$

    d. $3\left(\frac{5}{2} - y\right) + 2y = -3$

REMEMEBER TO CHECK YOUR ANSWERS WITH THE ANSWER KEY AND MAKE CORRECTIONS IN A DIFFERENT COLOR!!!