

i. Vocabulary:

1. Numbers that divide other numbers exactly are called Factors	2. The answer to a multiplication problem is called the products
3. The largest term that exactly divides given terms is called the G.C.F	4. The product of two equal factors is called a (n) Perfect Squares
5. A number that has more than 2 factors is called a (n) Composite	6. A method used to multiply two binomials double distribute box method
7. A polynomial of 3 terms is called trinomial	8. The standard form of a trinomial ax^2+bx+c

ii. Find the second factor of $36a^3b^2c$ if the first factor is:

9. $4a^2b$ $\frac{36a^3b^2c}{4a^2b}$ $9abc$	10. $-12a^3c$ $\frac{36a^3b^2c}{-12a^3c}$ $-3b^2$
11. $6abc$ $\frac{36a^3b^2c}{6abc}$ $6a^2b$	12. $-9abc$ $\frac{36a^3b^2c}{-9abc}$ $-4a^2b$

Identify the steps for factoring using the G.C.F Method:

- Determine the G.C.F (highest # : lowest exponent)
- Divide each term by the G.C.F
- put G.C.F on the outside: the quotient on the inside of the parenthesis
- check by distributing

iii. Write the following using the G.C.F method:

13.

$$\frac{7-35d}{7 \quad 7}$$
$$\boxed{7(1-5d)}$$

14.

$$\frac{27a^2bc+18ab^2c}{3abc \quad 3abc}$$
$$\boxed{3abc(9a+6b)}$$

15.

$$\frac{s^2r+s^3-s^4v}{s^2 \quad s^2 \quad s^2}$$
$$\boxed{s^2(r+s+s^2v)}$$

16.

$$\frac{10r-10s}{10 \quad 10}$$
$$\boxed{10(r-s)}$$

17.

$$\frac{4x+x^2}{x \quad x}$$
$$\boxed{x(4+x)}$$

18.

$$\frac{3x^2+6x+15}{3 \quad 3 \quad 3}$$
$$\boxed{3(x^2+2x+5)}$$

19.

$$\frac{ax+3x}{x \quad x}$$
$$\boxed{x(a+3)}$$

20.

$$\frac{xp+xq}{x \quad x}$$
$$\boxed{x(p+q)}$$

21.

$$\frac{7y-7}{7 \quad 7}$$
$$\boxed{7(y-1)}$$

22.

$$\frac{\pi r^2 - \pi r}{\pi r \quad \pi r}$$
$$\boxed{\pi r(r-1)}$$

- Identify the steps for factoring using the D.O.P.S Method:

- 1.) 2 set of parenthesis (+) (-)
- 2.) Take the square root of each perfect square
- 3.) Check by double distribute or box method

<p>23. $x^2 - 196$</p> $(x+14)(x-14)$	<p>24. $100 - d^2$</p> $(10-d)(10+d)$
<p>25. $4x^2 - 64y^2$</p> $(2x+8y)(2x-8y)$	<p>26. $\frac{25}{144} - 16y^4$</p> $\left(\frac{5}{12} + 4y^2\right)\left(\frac{5}{12} - 4y^2\right)$
<p>27. $x^{10} - 144$</p> $(x^5 - 12)(x^5 + 12)$	<p>28. $81 - y^8$</p> $(9 - y^4)(9 + y^4)$

29. Factored, the expression $16x^2 - 25y^2$ is equivalent to

$$(4x+5y)(4x-5y)$$

1) $(4x-5y)(4x+5y)$

2) $(4x-5y)(4x-5y)$

3) $(8x-5y)(8x+5y)$

4) $(8x-5y)(8x-5y)$

30. If Ann correctly factors an expression that is the difference of two perfect squares, her factors could be

D.O.T.S

1) $(2x+y)(x-2y)$

2) $(2x+3y)(2x-3y)$

3) $(x-4)(x-4)$

4) $(2y-5)(y-5)$

V. Write the product of the following:

<p>31. $(y-5)(y+5)$</p> $y^2 - 5y + 5y - 25$ $\boxed{y^2 - 25}$	<p>32. $(x+4)(x+3)$</p> $x^2 + 3x + 4x + 12$ $\boxed{x^2 + 7x + 12}$
<p>33. $(x-3)(x+2)$</p> $x^2 + 2x - 3x - 6$ $\boxed{x^2 - x - 6}$	<p>34. $(2x-3)(x+1)$</p> $2x^2 + 2x - 3x - 3$ $\boxed{2x^2 - x - 3}$

Identify the steps for factoring using the Easy Tri Method:

- 1.) a set of parenthesis is
- 2.) Determine the signs

If the last sign is a (+), then the signs are the same

If last sign is a (-), then the signs are different

- 3.) Determine the factors

If the last sign is a (+), then the factors you choose will be equal to the sum of the numerical coefficient of the middle term.

If the last sign is a (-) then the factors you choose will be equal to the difference of the numerical coefficient of the middle term.

- 4.) check by double distribute

<p>35. $x^2 + 8x + 15$</p> $\boxed{(x+3)(x+5)}$ <div style="text-align: right;"> $\begin{array}{r} 15 \\ \wedge \\ 1 \ 15 \\ \hline 3 \ 5 \end{array} = 8$ </div>	<p>36. $x^2 + 13x + 40$</p> $\boxed{(x+5)(x+8)}$ <div style="text-align: right;"> $\begin{array}{r} 40 \\ \wedge \\ 1 \ 40 \\ 2 \ 20 \\ 4 \ 10 \\ \hline 5 \ 8 \end{array}$ </div>
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37. $x^2 - 10x + 24$

$(x-4)(x-6)$

24
^
124
2 12
38
46

38. $x^2 - 15x + 36$

$(x-3)(x-12)$

36
^
136
218
312
49
66

39. $x^2 + 3x - 28$

$(x+7)(x-4)$

28
^
128
214
47

40. $x^2 - x - 6$

$(x-3)(x+2)$

6
^
16
23

41. What are the factors of $x^2 - 10x - 24$?

$(x-12)(x+2)$

$x^2 + 2x - 12x - 24$

$x^2 - 10x - 24$

- 1) $(x-4)(x+6)$
- 2) $(x-4)(x-6)$
- 3) $(x-12)(x+2)$
- 4) $(x+12)(x-2)$

24
^
124
38
46

42. What are the factors of $x^2 - 5x + 6$?

$(x-2)(x-3)$

$x^2 - 3x - 2x - 6$

$x^2 - 5x - 6$

- 1) $(x+2)$ and $(x+3)$
- 2) $(x-2)$ and $(x-3)$
- 3) $(x+6)$ and $(x-1)$
- 4) $(x-6)$ and $(x+1)$

6
^
16
23

43. What are the factors of the expression $x^2 + x - 20$?

$(x+5)(x-4)$

$x^2 - 4x + 5x - 20$

$x^2 + x - 20$

- 1) $(x+5)$ and $(x+4)$
- 2) $(x+5)$ and $(x-4)$
- 3) $(x-5)$ and $(x+4)$
- 4) $(x-5)$ and $(x-4)$

44. What is a common factor of $x^2 - 9$ and $x^2 - 5x + 6$?

$x^2 - 9 = (x-3)(x+3)$

$x^2 - 5x + 6 = (x-3)(x-2)$

- 1) $x+3$
- 2) $x-3$
- 3) $x-2$
- 4) x^2

Identify the steps for factoring using the Hard Tri Method:

- 1) Drop the 1st & last term
- 2) multiply the 1st & last term
- 3) Determine the factors & signs
- 4) Divide the G.C.F out on both binomials
- 5) keep the same binomials
- 6) put the G.C.Fs in the 2nd parenthesis
- 7) check by foiling

<p>45. $6x^2 + 11x - 10$</p> <p style="text-align: center;">60 14, 15</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> $\begin{array}{r l} 2x^2 + 15x & -4x - 10 \\ 3x & 3x \\ \hline 3x(2x+5) & -2(2x+5) \\ \hline \end{array}$ <p>same</p> </div> <div style="text-align: center;"> $\begin{array}{r l} 2x^2 + 2x & -3x - 3 \\ 2x & 2x \\ \hline 2x(x+1) & -3(x+1) \\ \hline \end{array}$ <p>same</p> </div> </div> <div style="border: 1px solid black; padding: 5px; margin-top: 10px; text-align: center;"> $(3x-2)(2x+5)$ </div>	<p>46. $2x^2 - x - 3$</p> <p style="text-align: center;">6 2, 3</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> $\begin{array}{r l} 2x^2 + 2x & -3x - 3 \\ 2x & 2x \\ \hline 2x(x+1) & -3(x+1) \\ \hline \end{array}$ <p>same</p> </div> </div> <div style="border: 1px solid black; padding: 5px; margin-top: 10px; text-align: center;"> $(2x-1)(x+1)$ </div>
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$47. \quad 4x^2 - 21x - 25$ <div style="text-align: center; margin-bottom: 10px;"> $\begin{matrix} 100 \\ \wedge \\ \boxed{4 \quad 25} \end{matrix}$ </div> $\begin{array}{c c} \frac{4x^2}{4x} + \frac{4x}{4x} & \frac{-25x}{-25} - \frac{25}{-25} \\ \hline & \end{array}$ $4x(x+1) \quad -25(x+1)$ <p style="text-align: center; margin-left: 100px;"><u>same</u></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $(4x - 25)(x + 1)$ </div>	$48. \quad 3x^2 - 4x - 4$ <div style="text-align: center; margin-bottom: 10px;"> $\begin{matrix} 12 \\ \wedge \\ \boxed{2 \quad 6} \end{matrix}$ </div> $\begin{array}{c c} \frac{3x^2}{3x} - \frac{6x}{3x} & \frac{+2x}{2} - \frac{4}{2} \\ \hline & \end{array}$ $3x(x-2) \quad 2(x-2)$ <p style="text-align: center; margin-left: 100px;"><u>same</u></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $(3x + 2)(x - 2)$ </div>
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WHEN FACTORING YOU ALWAYS LOOK FOR G.C.F

$49. \quad 2x^2 - 72y^2$ <p style="margin-left: 20px;">$\frac{2}{2} \quad \frac{72}{2} \quad \text{G.C.F}$</p> $2(x^2 - 36y^2) \text{ DOTS}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $2(x - 6y)(x + 6y)$ </div>	$50. \quad 2x^2 - 8x - 10$ <p style="margin-left: 20px;">$\frac{2}{2} \quad \frac{8}{2} \quad \frac{10}{2} \quad \text{G.C.F}$</p> $2(x^2 - 4x - 5) \text{ EASY}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $2(x - 5)(x + 1)$ </div>
$51. \quad 5x^2 - 20$ <p style="margin-left: 20px;">$\frac{5}{5} \quad \frac{20}{5} \quad \text{G.C.F}$</p> $5(x^2 - 4) \text{ DOTS}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $5(x - 2)(x + 2)$ </div>	$52. \quad 3x^2 - 75x$ <p style="margin-left: 20px;">$\frac{3}{3} \quad \frac{75}{3} \quad \text{G.C.F}$</p> $3(x^2 - 25) \text{ DOTS}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $3(x + 5)(x - 5)$ </div>

53. $6x^2 - 6x^4$

$6x^2 \ 6x^2$

$6x^2(1 - x^2)$

$6x^2(1-x)(1-x)$

54. $x - 25x^3$

$x \ x \ G.C.F$

$x(1 - 25x^2)$ DOPS

$x(1-5x)(1+5x)$

55. $5x^2 + 15x + 10$

$5 \ 5 \ 5 \ G.C.F$

$5(x^2 + 3x + 2)$ easy tri

$5(x+1)(x+2)$

56. $ax^2 - 18ax + 77a$

$a \ a \ a \ G.C.F$

$a(x^2 - 18x + 77)$ easy tri

$a(x-7)(x-11)$

57. Factored completely, the expression $2y^2 + 12y - 54$ is equivalent to

$2 \ 2 \ 2$

1) $2(y+9)(y-3)$

2) $2(y-3)(y-9)$

3) $(y+6)(2y-9)$

4) $(2y+6)(y-9)$

$2(y^2 + 6y - 27)$

$2(y+9)(y-3)$

58. Factored completely, the expression $2x^2 + 10x - 12$ is equivalent to

$2 \ 2 \ 2$

1) $2(x-6)(x+1)$

2) $2(x+6)(x-1)$

3) $2(x+2)(x+3)$

4) $2(x-2)(x-3)$

$2(x^2 + 5x - 6)$

$2(x+6)(x-1)$

59. Which expression represents $36x^2 - 100y^6$ factored completely?

$4 \ 4$

1) $2(9x + 25y^3)(9x - 25y^3)$

2) $4(3x + 5y^3)(3x - 5y^3)$

3) $(6x + 10y^3)(6x - 10y^3)$

4) $(18x + 50y^3)(18x - 50y^3)$

$4(9x^2 - 25y^6)$

$4(3x - 5y^3)(3x + 5y^3)$

60. Written in simplest factored form, the binomial $2x^2 - 50$ can be expressed as

1) $2(x-5)(x-5)$

2) $2(x-5)(x+5)$

3) $(x-5)(x+5)$

4) $2x(x-50)$

$2x^2 - 50$

$2(x^2 - 25)$

$2(x+5)(x-5)$