

DO NOW:

<p>a) Create a perfect square trinomial and factor it:  <math>x^2 + 10x + 25</math>  <math>(x + 5)^2</math></p>	<p>b) Create a perfect square trinomial and factor it:  <math>x^2 - 10x + 25</math>  <math>(x - 5)^2</math></p>
<p>c) Solve for the roots <math>x^2 = 36</math>  <math>x = \pm 6</math></p>	<p>d) Solve for x-intercepts <math>x^2 + 6x - 16 = 0</math>  <math>(x + 8)(x - 2) = 0</math>  <math>x = -8 \quad   \quad x = 2</math>  <math>\{-8, 2\}</math></p>

AIM: COMPLETING THE SQUARE (a = 1)

1. Let's solve  $x^2 + 6x - 16 = 0$  another way!!

b-value:  
 $\frac{6}{2} = (3)^2 = 9$

$$\begin{aligned}
 & \begin{array}{r} +16 + 16 \\ \hline x^2 + 6x = 16 \end{array} \\
 & x^2 + 6x + 9 = 16 + 9 \\
 & (x + 3)(x + 3) = 25 \\
 & \sqrt{(x + 3)^2} = \sqrt{25} \\
 & x + 3 = \pm 5 \\
 & \begin{array}{r} x + 3 = 5 \\ \hline x = 2 \end{array} \quad \begin{array}{r} x + 3 = -5 \\ \hline x = -8 \end{array} \quad \{-2, -8\}
 \end{aligned}$$

Completing the Square is used when: when you can not factor the quadratic equation

2. Solve for the roots in simplest radical form:  $x^2 + 8x - 4 = 0$

b-value:

$$\frac{8}{2} = (4)^2 = \boxed{16}$$

$$x^2 + 8x = \overset{+4+4}{4}$$

$$x^2 + 8x + 16 = 4 + 16$$

$$(x+4)(x+4) = 20$$

$$\sqrt{(x+4)^2} = \sqrt{20}$$

$$x+4 = \sqrt{4} \sqrt{5}$$

$$x+4 = \pm 2\sqrt{5}$$

$$x+4 = 2\sqrt{5}$$

$$\begin{array}{r} -4 \\ -4 \\ \hline x = -4 + 2\sqrt{5} \end{array}$$

$$x+4 = -2\sqrt{5}$$

$$\begin{array}{r} -4 \\ -4 \\ \hline x = -4 - 2\sqrt{5} \end{array}$$

- |   |
|---|
| 1) Move the constant ("c" value) to the right side. (The "a" value must be equal to 1!)       |
| 2) Make the left side a perfect square trinomial: Take half of the "b" value.                 |
| 3) Square it.   |
| 4) Add it to BOTH sides.  |
| 5) Factor the perfect square trinomial and simplify right side.                               |
| 6) Take the square root of both sides and solve! (Remember positive and negative results!!!!) |

$$\{-4 \pm 2\sqrt{5}\}$$

3. Find the zeros of the function in simplest radical form:  $x^2 + 20x = -40$

b-value:

$$\frac{20}{2} = (10)^2 = \boxed{100}$$

$$x^2 + 20x + 100 = -40 + 100$$

$$(x+10)(x+10) = 60$$

$$\sqrt{(x+10)^2} = \sqrt{60}$$

$$x+10 = \pm \sqrt{4} \sqrt{5}$$

$$x+10 = \pm 2\sqrt{5}$$

$$\begin{array}{r} -10 \\ -10 \\ \hline x = -10 \pm 2\sqrt{5} \end{array}$$

$$\{-10 \pm 2\sqrt{5}\}$$

4. Find the solution set by completing the square:  $x^2 - 6x = 18$

b-value:

$$\frac{-6}{2} = (-3)^2 = 9 \quad x^2 - 6x + 9 = 18 + 9$$

$$(x - 3)(x - 3) = 27$$

$$(x - 3)^2 = 27$$

$$\sqrt{x - 3} = \pm \sqrt{27}$$

$$x - 3 = \pm \sqrt{9} \sqrt{3}$$

$$x - 3 = \pm 3\sqrt{3}$$

$$\begin{array}{r} +3 \quad +3 \\ \hline x = 3 \pm 3\sqrt{3} \end{array}$$

- |   |
|---|
| 1. Move the constant ("c" value) to the right side.<br>(The "a" value must be equal to 1!)    |
| 2. Make the left side a perfect square trinomial: Take half of the "b" value.                 |
| 3. Square it.   |
| 4. Add it to BOTH sides.  |
| 5. Factor the perfect square trinomial and simplify right side.                               |
| 6. Take the square root of both sides and solve! (Remember positive and negative results!!!!) |

5. Solve for the roots by completing the square in simplest radical form:  $x^2 - 4x = 1$

b-value:

$$\frac{-4}{2} = (-2)^2 = 4 \quad x^2 - 4x + 4 = 1 + 4$$

$$(x - 2)(x - 2) = 5$$

$$\sqrt{(x - 2)^2} = \sqrt{5}$$

$$x - 2 = \pm \sqrt{5}$$

$$\begin{array}{r} +2 \quad +2 \\ \hline x = 2 \pm \sqrt{5} \end{array}$$

$$\{ 2 \pm \sqrt{5} \}$$