

Do Now:

- a. If one root of the equation  $x^2 + kx - 15 = 0$  is -3, what is the other root?

$$(-3)^2 + k(-3) - 15 = 0$$

$$9 - 3k - 15 = 0$$

$$-6 - 3k = 0$$

$$\begin{array}{r} +3k \\ +3k \end{array}$$

$$\frac{-6}{3} = \frac{3k}{3}$$

$$-2 = k$$

$$\begin{array}{l} x = -3 \\ x^2 + kx - 15 = 0 \\ x^2 - 2x - 15 = 0 \\ (x - 5)(x + 3) = 0 \\ \boxed{x = 5} \quad | \quad x = -3 \end{array}$$

- b. Using your calculator, find the axis of symmetry and the turning point of  $f(x) = x^2 + 4x - 21$ .

$$(-2, -25) \rightarrow \text{T.P.}$$

$$x = -2 \rightarrow \text{A.O.S.}$$

### AIM: FINDING THE AXIS OF SYMMETRY AND TURNING POINT ALGEBRAICALLY

Other words for turning point: vertex, maximum, minimum, Turning Point

Directions: Find the turning point *algebraically*.

1.  $g(x) = x^2 + 4x - 21$

$$a = 1 \quad x = -\frac{b}{2a} = -\frac{4}{2}$$

$$b = 4$$

$$\boxed{x = -2} \quad \text{x-value of T.P.}$$

$$g(x) = x^2 + 4x - 21$$

$$g(2) = (2)^2 + 4(2) - 21$$

$$\boxed{g(2) = -25} \quad \text{y-value of T.P.}$$

$$(-2, -25) \rightarrow \text{vertex}$$

Step 1: Identify the a-value & b-value

Step 2: Use the axis of symmetry formula:

$$x = \frac{-b}{2a}$$

Step 3: Plug the x-value into the given equation to find the y-value.

$$y = ax^2 + bx + c$$

Step 4: Write your answer as coordinates.

Step 5: Check your answer with the table/graph on the calculator

2. Find the vertex algebraically.  $h(x) = -x^2 - 10x + 24$

$$a = -1 \quad x = -\frac{(-10)}{2(-1)} = \frac{10}{-2}$$
$$b = -10$$

$$\boxed{x = -5} \rightarrow x\text{-value of T.P.}$$

$$h(x) = -x^2 - 10x + 24$$

$$h(-5) = -(-5)^2 - 10(-5) + 24$$

$$\boxed{h(-5) = 49} \rightarrow y\text{-value of T.P.}$$

$$(-5, 49) \rightarrow \text{vertex}$$

Step 1: Identify the a-value & b-value

Step 2: Use the axis of symmetry formula:

$$x = \frac{-b}{2a}$$

Step 3: Plug the x-value into the given equation to find the y-value.

$$y = ax^2 + bx + c$$

Step 4: Write your answer as coordinates.

Step 5: Check your answer with the table/graph on the calculator

3. Find the minimum point algebraically:  $a(x) = x^2 + 6x - 27$

$$a = 1 \quad x = -\frac{(6)}{2(1)} = -\frac{6}{2}$$
$$b = 6$$

$$\boxed{x = -3} \rightarrow x\text{-value of T.P.}$$

$$a(x) = x^2 + 6x - 27$$

$$a(-3) = (-3)^2 + 6(-3) - 27$$

$$\boxed{a(-3) = -36} \rightarrow y\text{-value of T.P.}$$

$$(-3, -36) \rightarrow \text{vertex}$$

Step 1: Identify the a-value & b-value

Step 2: Use the axis of symmetry formula:

$$x = \frac{-b}{2a}$$

Step 3: Plug the x-value into the given equation to find the y-value.

$$y = ax^2 + bx + c$$

Step 4: Write your answer as coordinates.

Step 5: Check your answer with the table/graph on the calculator

4. Find the vertex algebraically:  $b(x) = x^2 + 8x + 16$

$a=1$        $x = -\frac{(8)}{2(1)} = -\frac{8}{2}$   
 $b=8$

$x = -4 \rightarrow x\text{-value of T.P.}$

$b(x) = x^2 + 8x + 16$

$b(-4) = (-4)^2 + 8(-4) + 16$

$b(-4) = 0 \rightarrow y\text{-value of T.P.}$

$(-4, 0) \rightarrow \text{vertex}$

Step 1: Identify the a-value & b-value

Step 2: Use the axis of symmetry formula:

$$x = \frac{-b}{2a}$$

Step 3: Plug the x-value into the given equation to find the y-value.

$$y = ax^2 + bx + c$$

Step 4: Write your answer as coordinates.

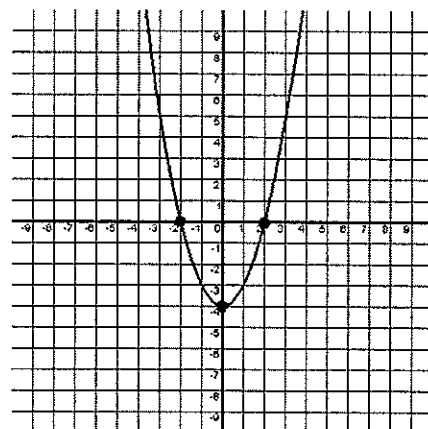
Step 5: Check your answer with the table/graph on the calculator

5) Write the quadratic equation given the graph below.

$x = -2$  |  $x = 2$   
 $(x+2)$  |  $(x-2) = 0$

$x^2 - 2x + 2x - 4 = y$

$x^2 - 4 = y$



6) If -1 and 7 are the roots of the quadratic equation  $x^2 + kx - 7 = 0$ , find the value of  $k$

$x = -1$  |  $x = 7$   
 $(x+1)$  |  $(x-7) = 0$

$x^2 - 7x + 1x - 7 = 0$

$x^2 - 6x - 7 = 0$

$k = -6$